

# AN FPGA-BASED IMPLEMENTATION OF A HYPERSPECTRAL ANOMALY DETECTION ALGORITHM FOR REAL-TIME APPLICATIONS

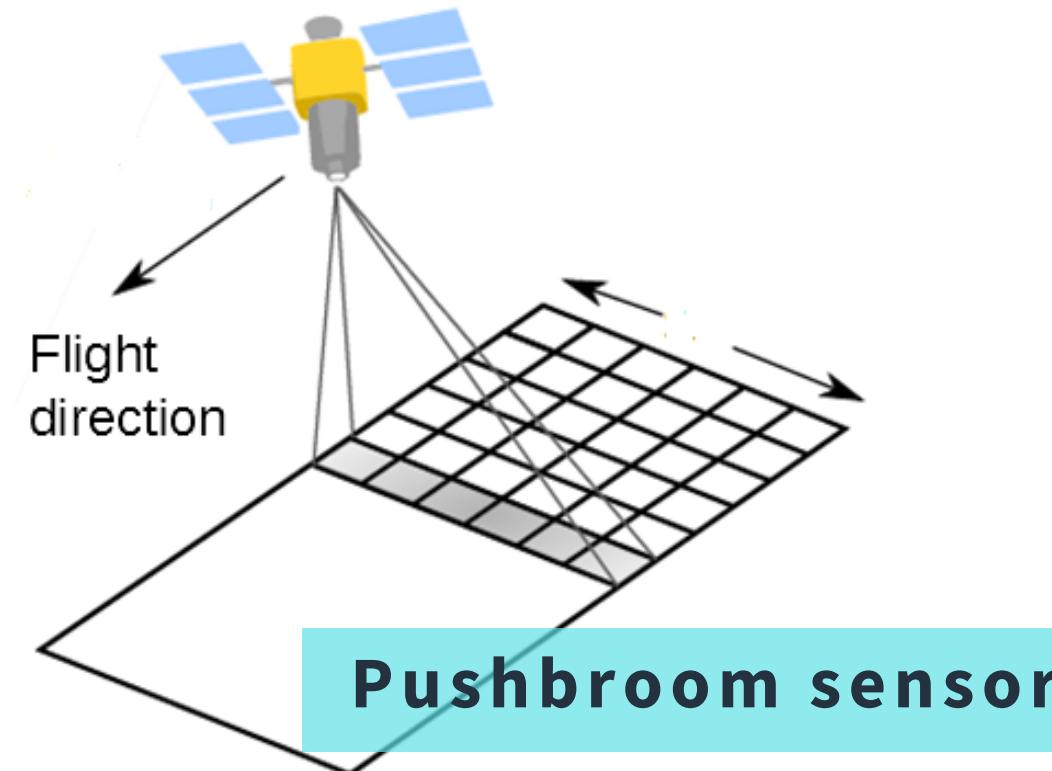
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## Authors:

María Díaz Martín, Julián Caba, Raúl Guerra Hernández, Jesús Barba, Sebastián López Suárez

# MOTIVATIONS

Sensor	Pixels per frame	Bands per frame	Frames per second	Data resolution
SPECIM FX-10	1024	240/160	330	12 bits/ 16 bits packaged

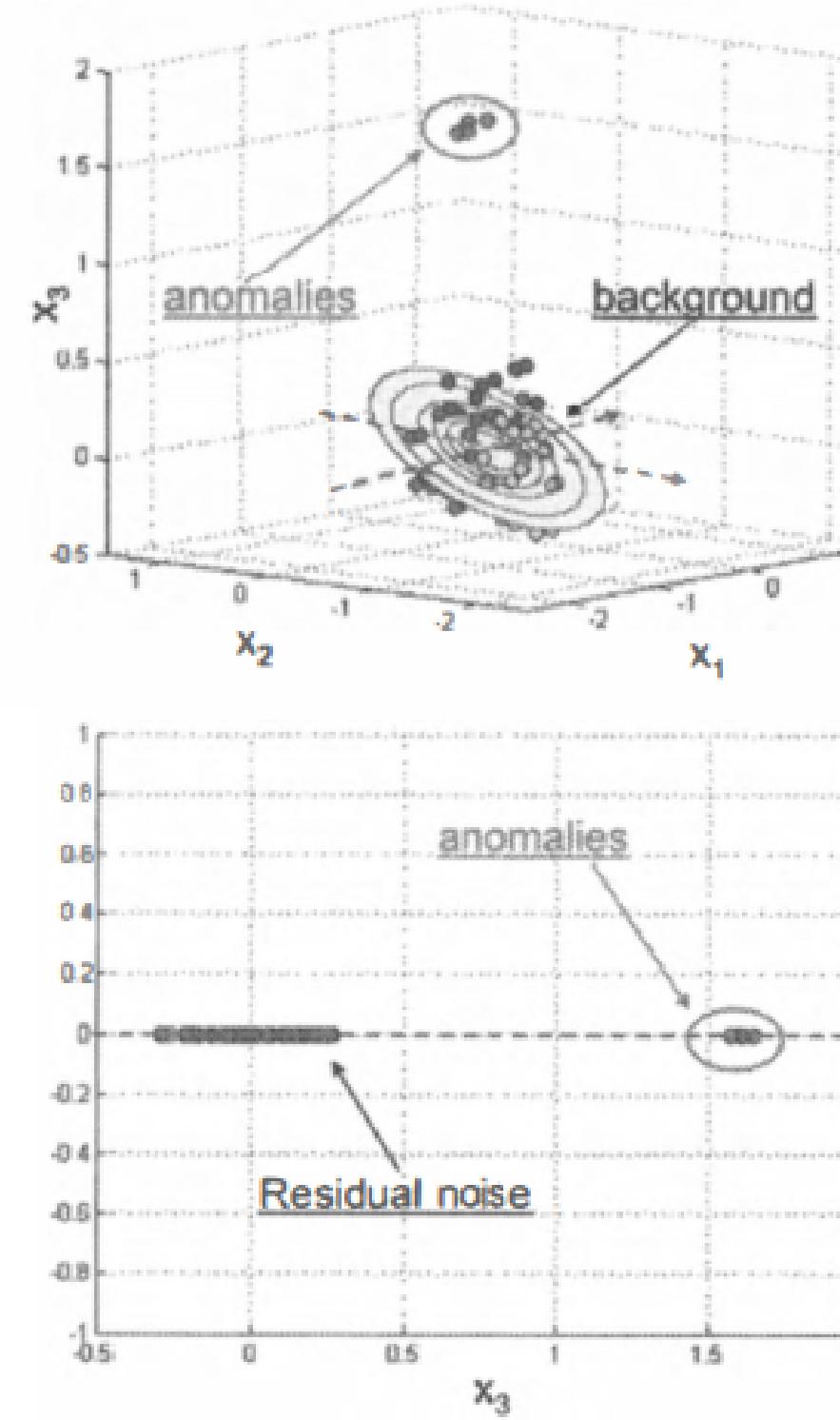


- More than 9 GB/min to be processed
- Line-by-line performance
- Short battery life
- Low-power, low-cost, low-weight and compact size onboard PC



ZedBoard  
(Xilinx Zynq-7020 SoC)

# SUBSPACE ANOMALY DETECTION



$$\mathbf{r}_j = \sum_{n=1}^p \mathbf{e}_n \cdot a_{j,n} + \mathbf{n}_j$$

!   
   **$\mathbf{b}_n$**  = background spectra  
   **$\mathbf{s}$**  = desired target (??)

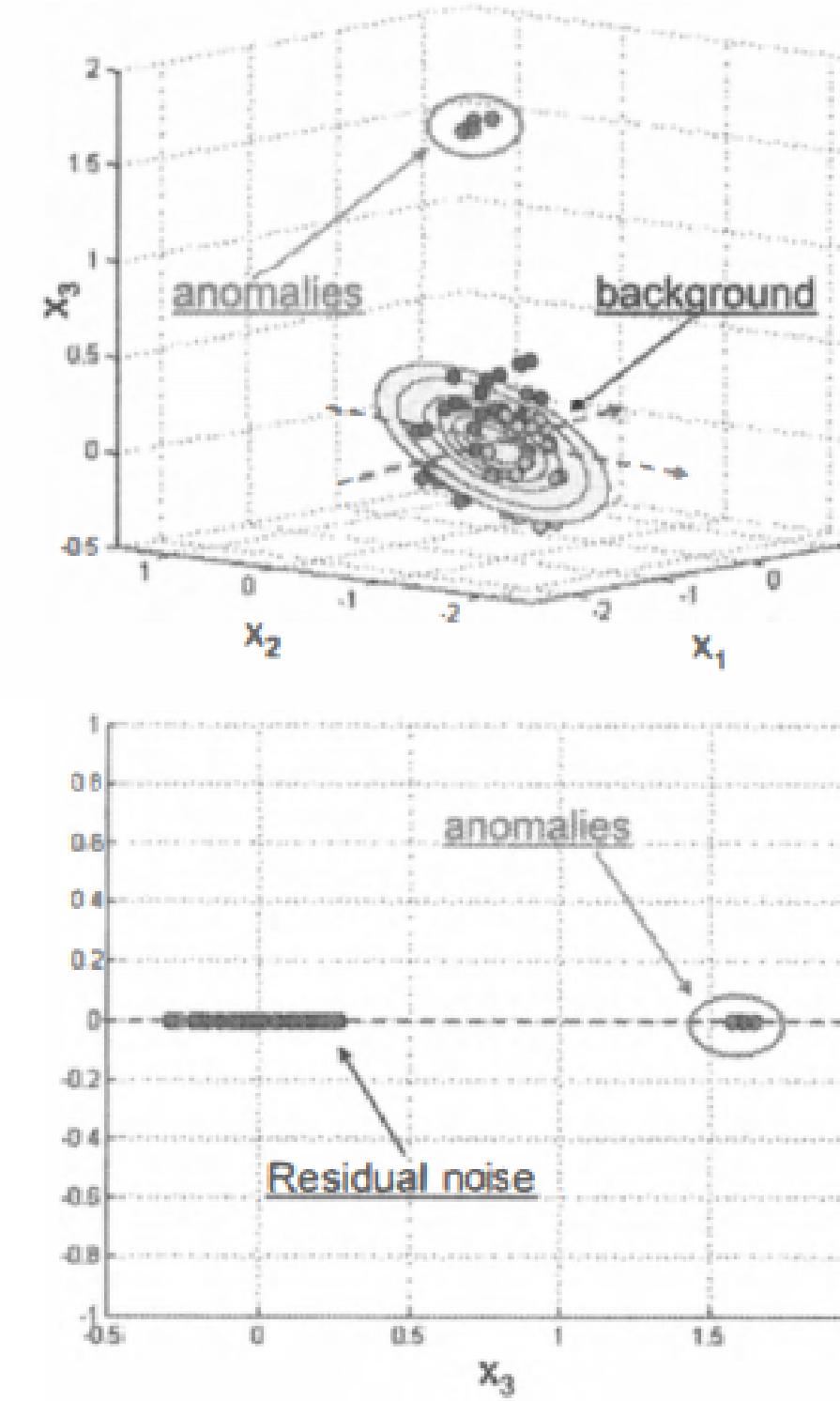
$$\mathbf{r}_j = \sum_{n=1}^p \mathbf{b}_n \cdot a_{j,n} + \mathbf{s} \cdot a_{sj} + \mathbf{n}_j$$

!   
  *Orthogonal subspace  
projection (OSP)*

$$\mathbf{d} = (\mathbf{r}_j - \hat{\mu}_b)' \cdot \mathbf{P} \cdot (\mathbf{r}_j - \hat{\mu}_b)$$

Images taken from Matteoli S. et al. DOI:10.1109/MAES.2010.5546306.

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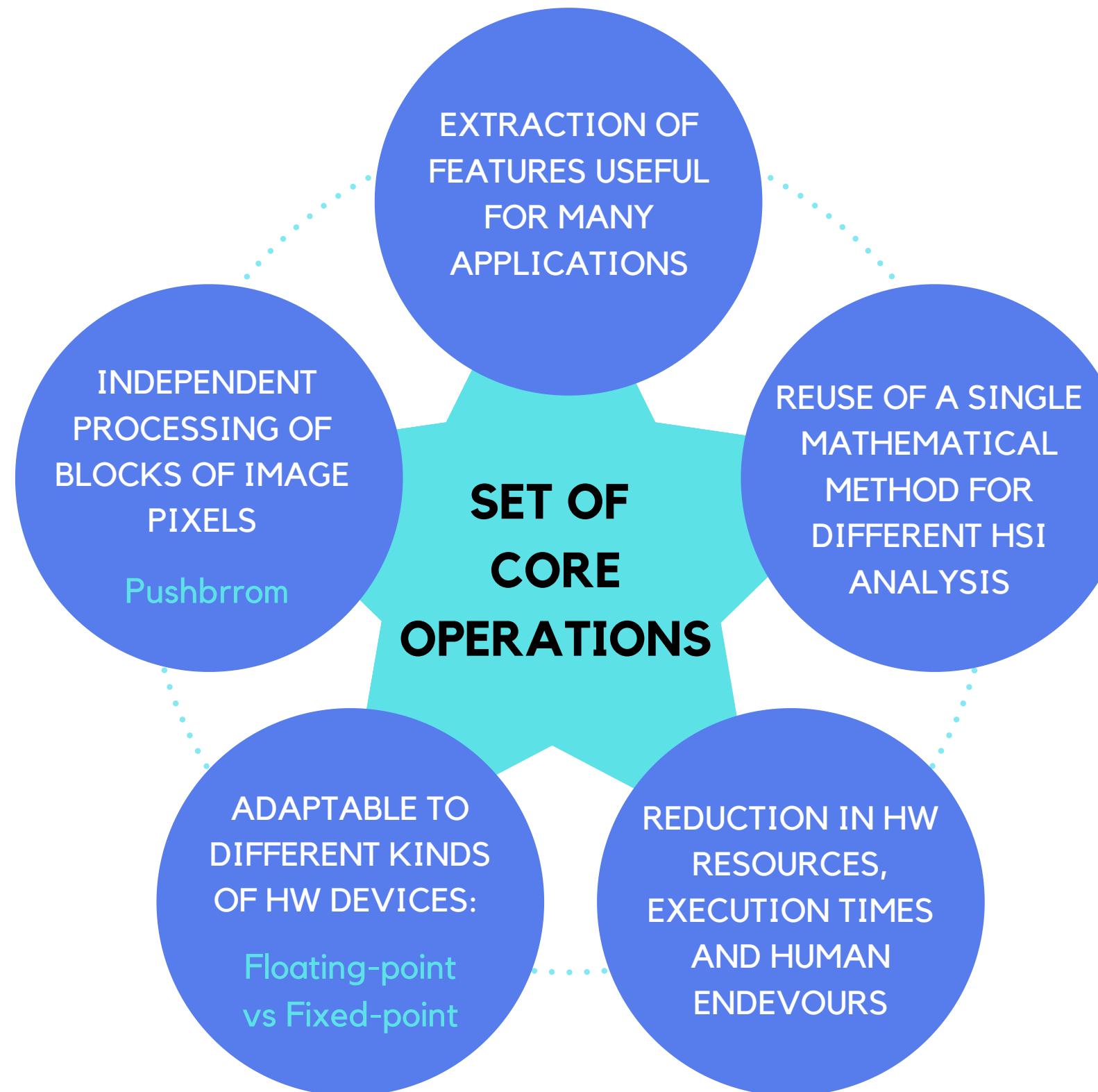
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# SET OF CORE OPERATIONS

INTRODUCTION  
SET OF CORE OPERATIONS



03

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# SET OF CORE OPERATIONS

**Inputs:**

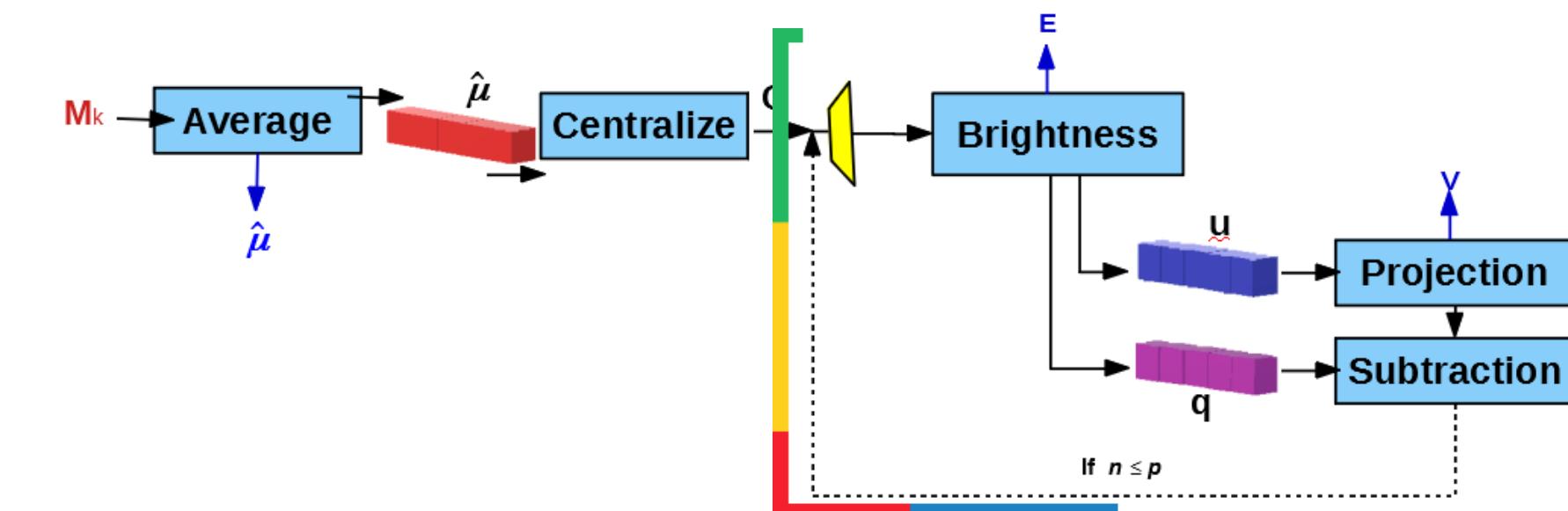
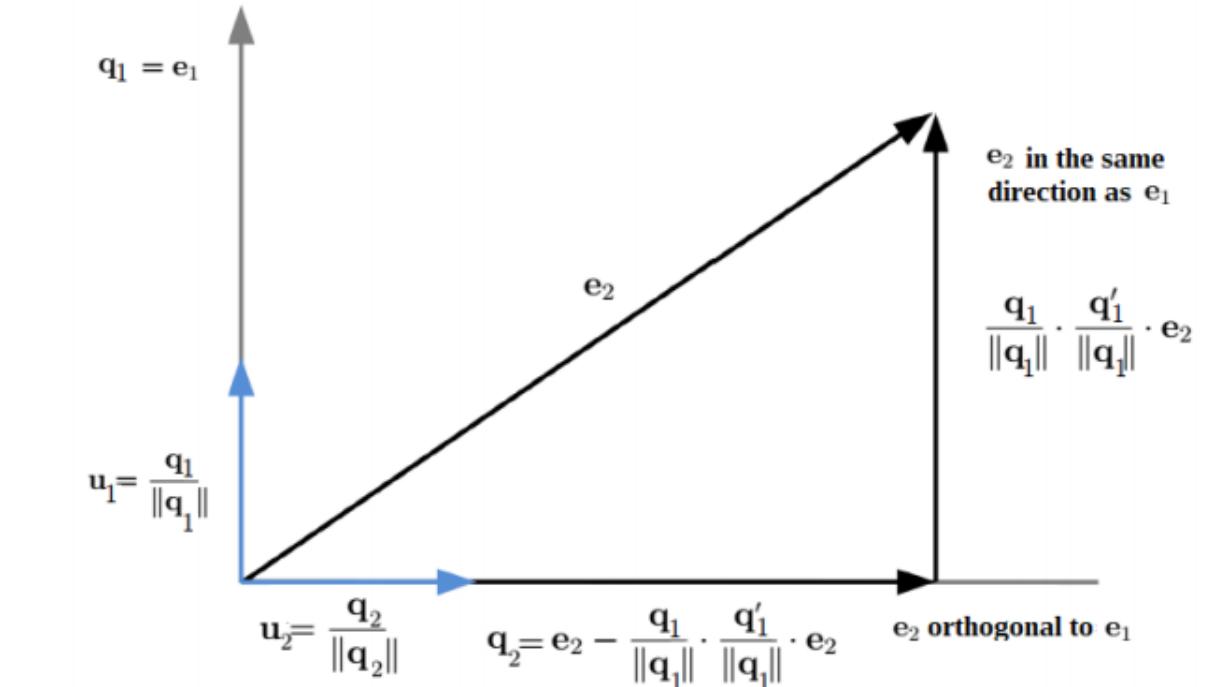
$$\mathbf{M}_k = [\mathbf{r}_1, \mathbf{r}_2, \dots, \mathbf{r}_{BS}]$$

**Outputs:**

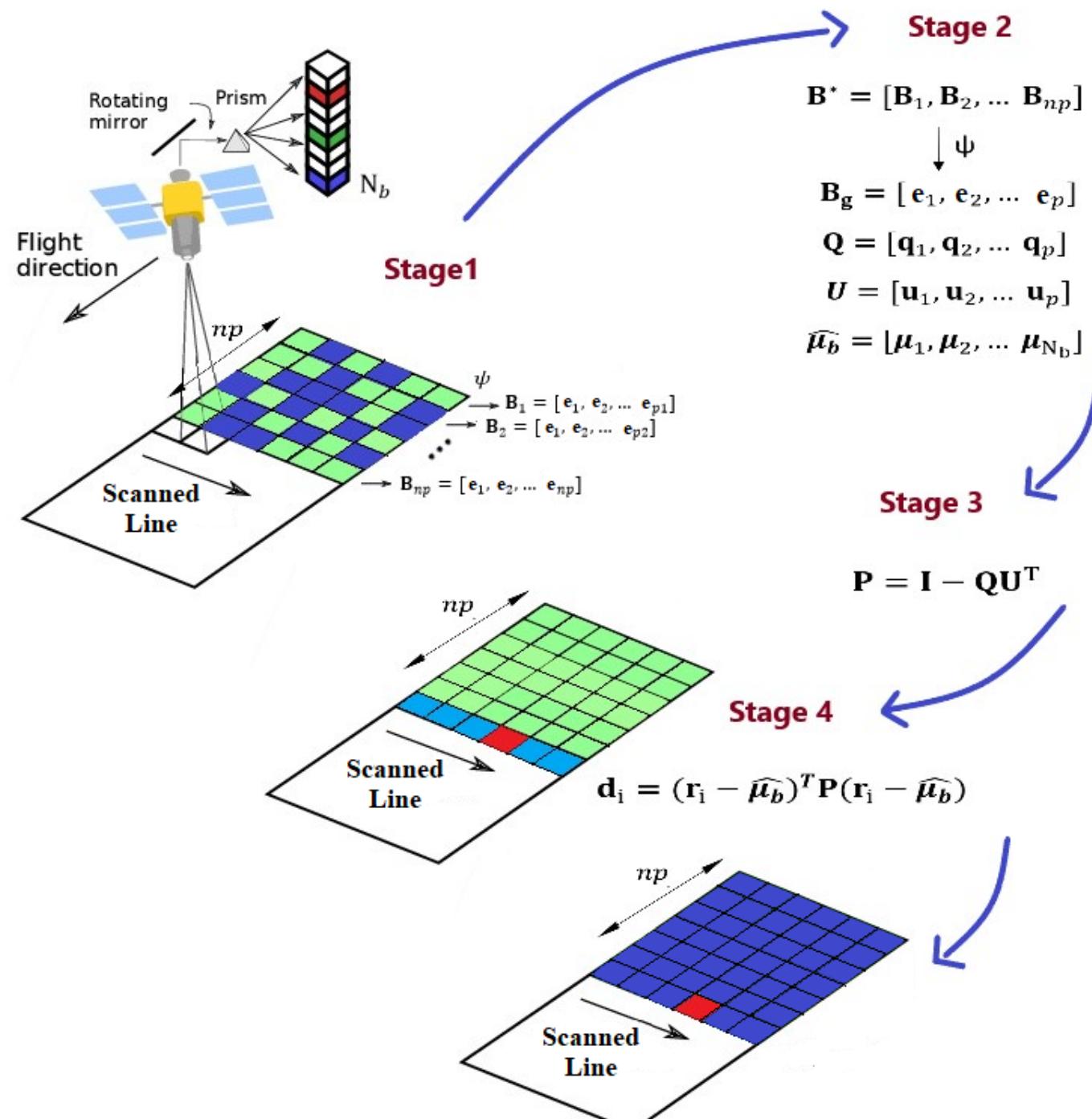
$$\begin{aligned} \hat{\mu} & \text{ {Average Pixel}}; \quad \mathbf{E} = [\mathbf{e}_1, \mathbf{e}_2, \dots, \mathbf{e}_p] \text{ {Characteristic pixels}}; \quad \mathbf{Q} = [\mathbf{q}_1, \mathbf{q}_2, \dots, \mathbf{q}_p] \\ & \text{ {Orthogonalized vectors}}; \quad \mathbf{U} = [\mathbf{u}_1, \mathbf{u}_2, \dots, \mathbf{u}_p] \text{ {Orthonormalized vectors}}; \quad \mathbf{V} = \\ & [\mathbf{v}_1, \mathbf{v}_2, \dots, \mathbf{v}_p] \text{ {Projection vectors}} \end{aligned}$$

**Algorithm:**

- 1: Average pixel:  $\hat{\mu}$ ;
- 2: Centralization:  $\mathbf{C} = \mathbf{M}_k - \hat{\mu}$ ;
- 3: **for**  $n = 1$  **to**  $p$  **do**
- 4:     **for**  $j = 1$  **to**  $BS$  **do**
- 5:         Brightness Calculation:  $\mathbf{b}_j = \mathbf{c}'_j \cdot \mathbf{c}_j$ ;
- 6:     **end for**
- 7:     Maximum Brightness:  $j_{max} = \text{argmax}(\mathbf{b}_j)$ ;
- 8:     Extracted pixels:  $\mathbf{e}_n = \mathbf{r}_{j_{max}}$ ;
- 9:      $\mathbf{q}_n = \mathbf{c}_{j_{max}}$ ;
- 10:     $\mathbf{u}_n = \mathbf{q}_n / b_{j_{max}}$ ;
- 11:    Projection:  $\mathbf{v}_n = \mathbf{u}'_n \cdot \mathbf{C}$ ;
- 12:    Subtraction:  $\mathbf{C} = \mathbf{C} - \mathbf{q}_n \cdot \mathbf{v}_n$ ;
- 13: **end for**



# THE HW-LbL-FAD



Background estimation

Stage 1

Stage 2

Stage 3

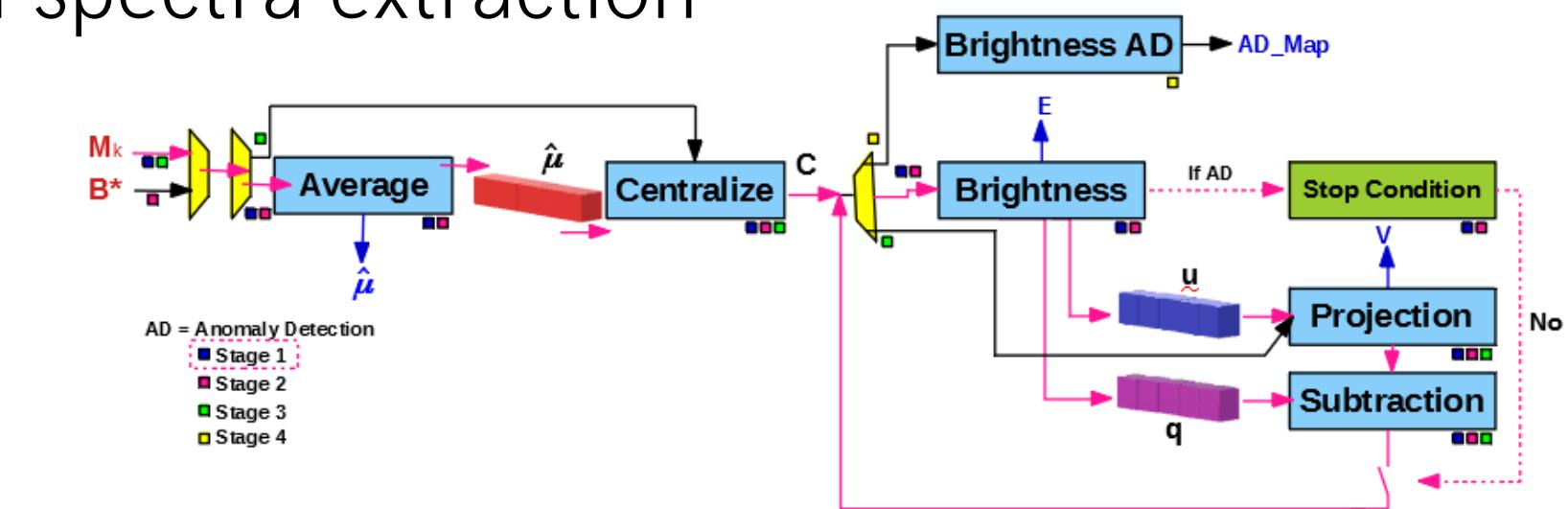
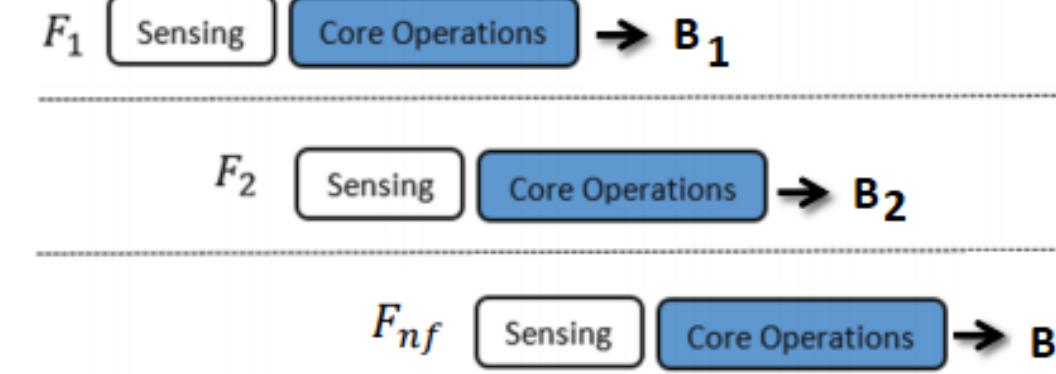


Anomaly detection

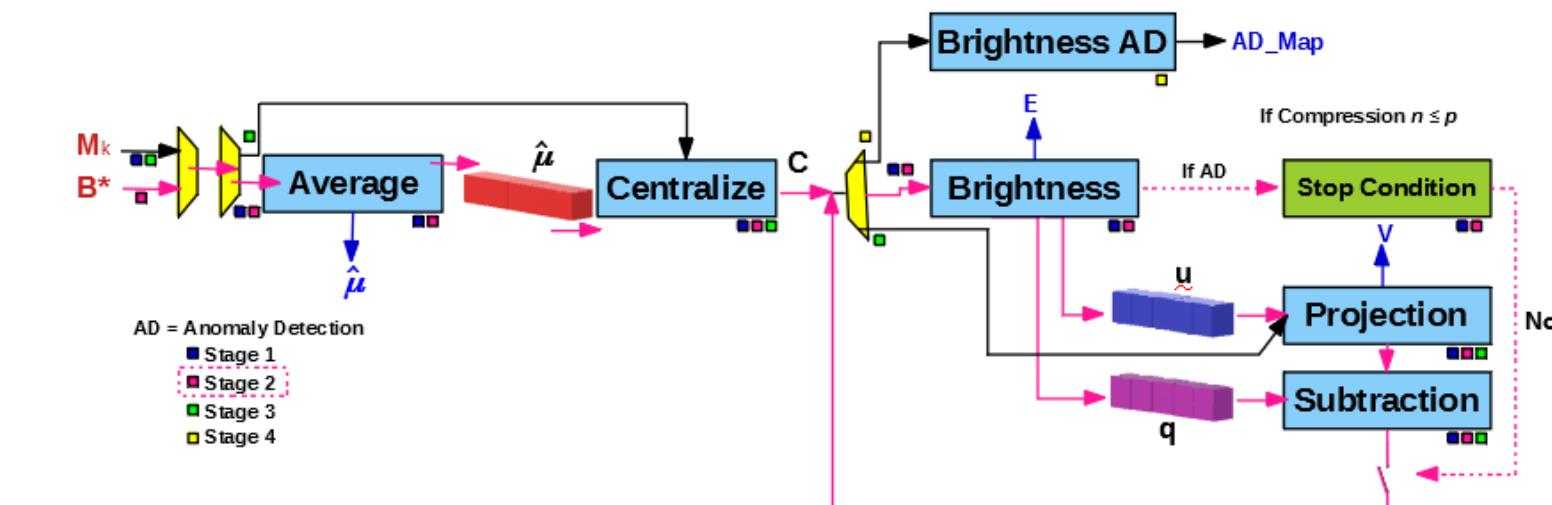
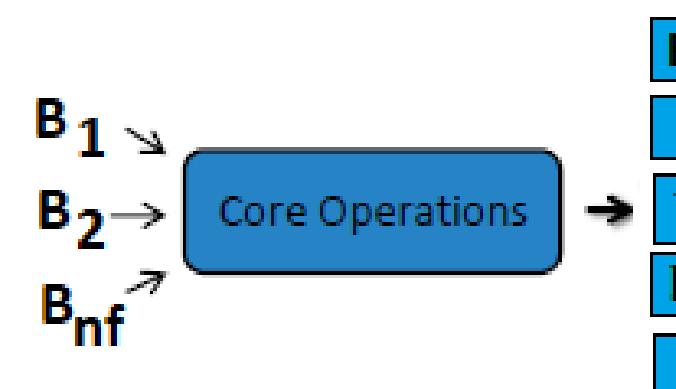
Stage 4

## Background estimation

### Stage 1: Line-by-line background spectra extraction



### Stage 2: Overall background subspace estimation



# THE HW-LbL-FAD



## *Background estimation*

- Stage 3: Orthogonal Subspace to the one spanned by the background Samples

$$P = I - \frac{W \cdot W'}{W' \cdot W}; Q = W; U = \frac{W}{W' \cdot W} \longrightarrow P = I - Q \cdot U$$



## *Anomaly detection*

- Stage 4: Detection of anomalies

$$\text{d} = (\mathbf{r}_j - \hat{\mu}_b)' \cdot \mathbf{P} \cdot (\mathbf{r}_j - \hat{\mu}_b) \longrightarrow \text{Threshold} \rightarrow 1,5 \cdot \tau$$



## Background estimation

- Stage 3: Orthogonal Subspace to the one spanned by the background Samples

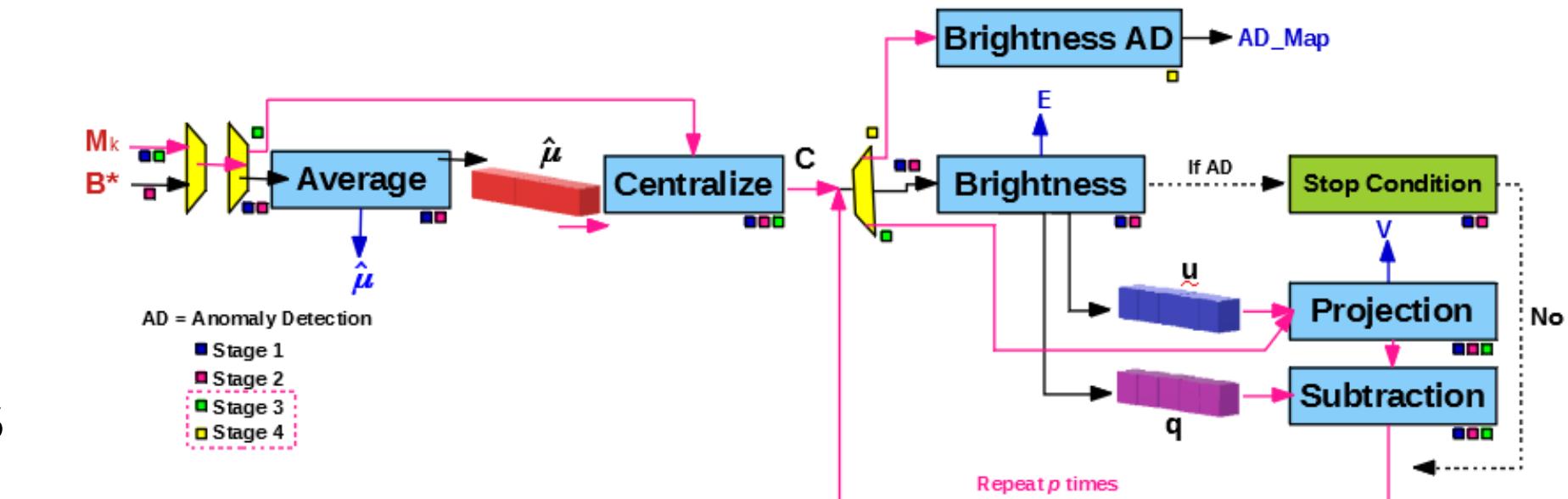
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## Anomaly detection

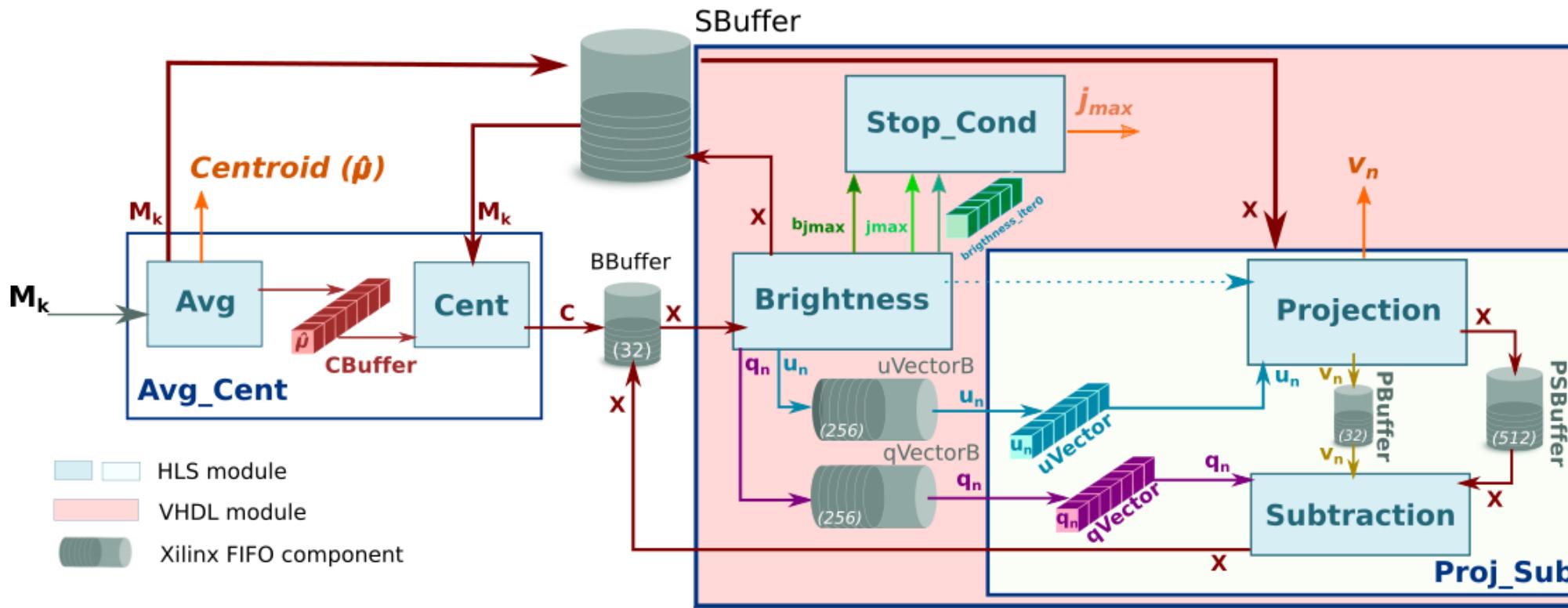
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# FPGA-BASED IMPLEMENTATION

FPGA-BASED IMPLEMENTATION  
SET OF CORE OPERATIONS



## Set of Core operations

Avg\_Cent, Brightness, Proj\_Sub,  
Stop\_cond ---> HLS

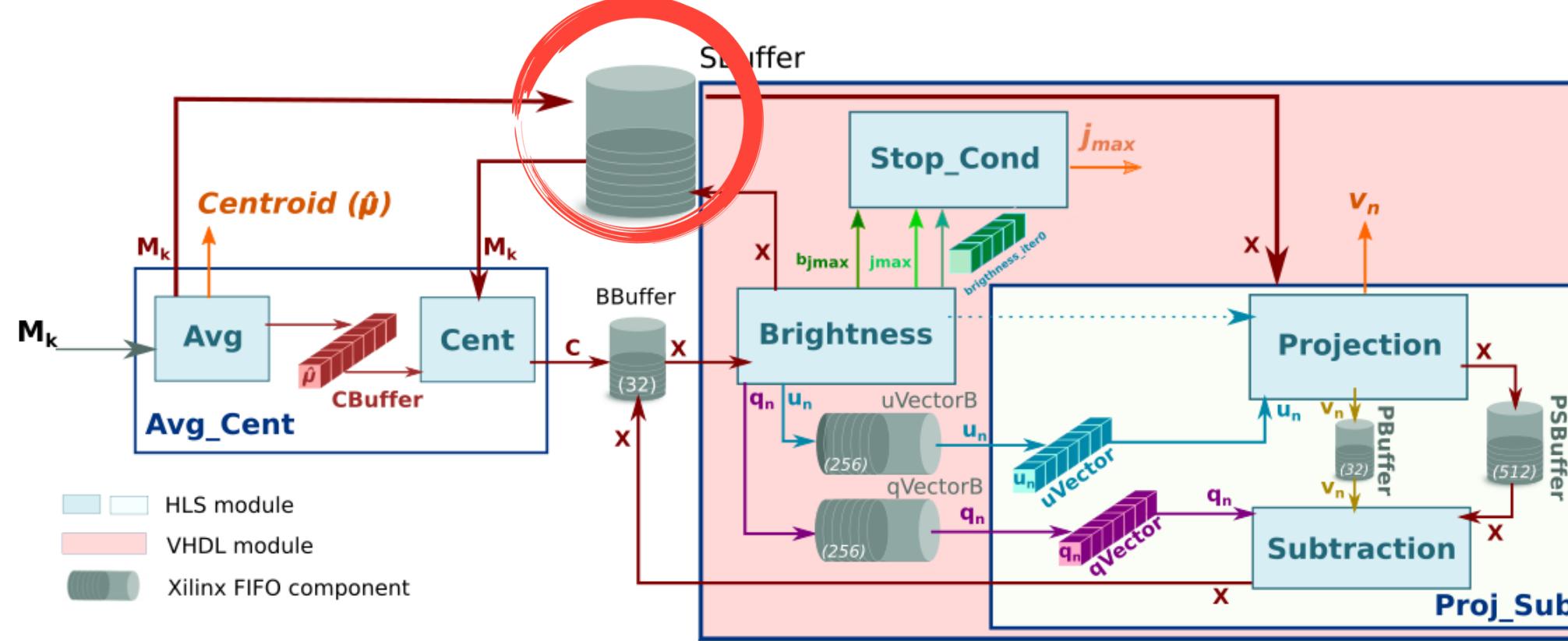
Glue logic + memory  
elements + FSM ---> VHDL

Hybrid solution  
HLS + VHDL

# FPGA-BASED IMPLEMENTATION

FPGA - BASED IMPLEMENTATION

SET OF CORE OPERATIONS



Set of Core operations

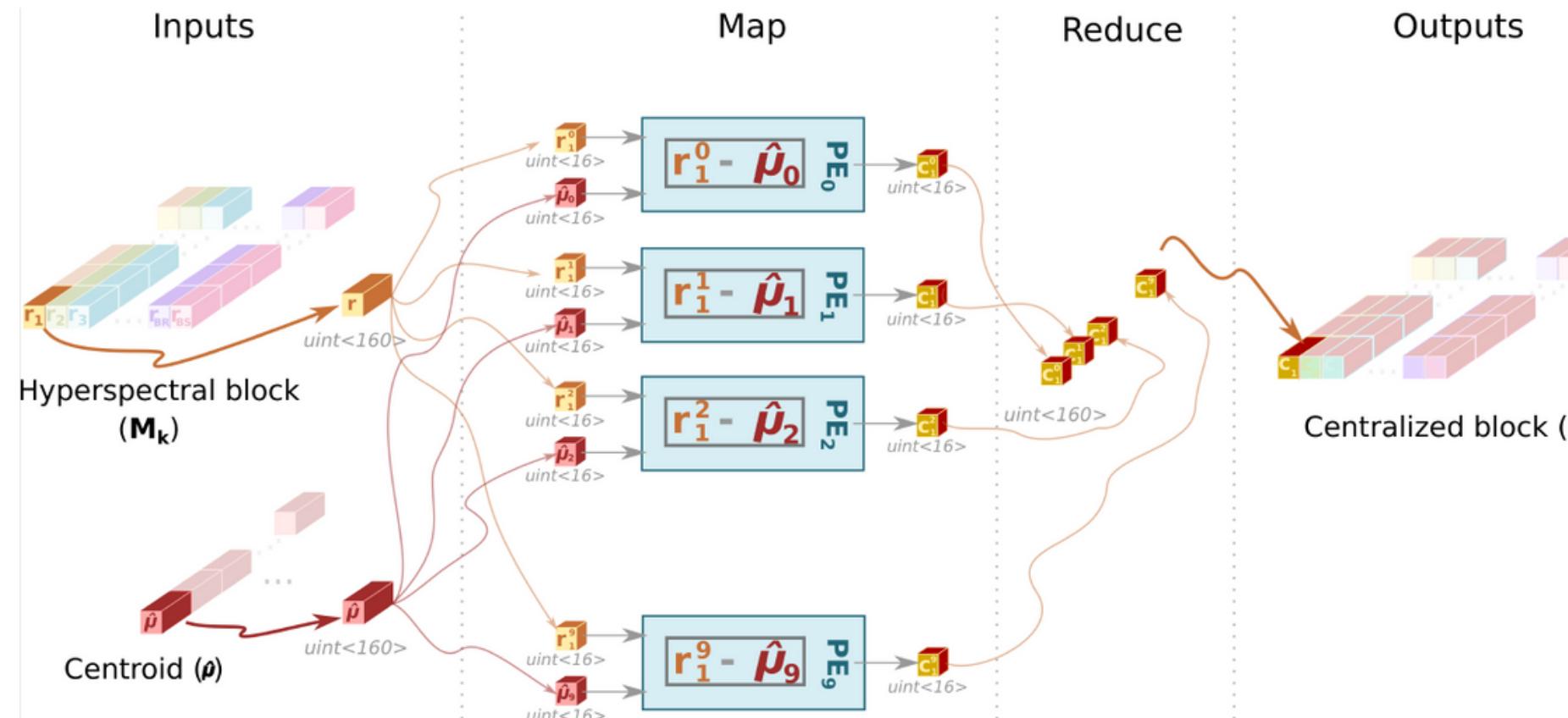
Avg\_Cent, Brightness, Proj\_Sub,  
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Glue logic + memory  
elements + FSM ---> VHDL

Depends on BS and bit-depth ---> Design time

Hybrid solution  
HLS + VHDL

# FPGA-BASED IMPLEMENTATION



Map-reduce programming model --- > PEs

## Set of Core operations

Avg\_Cent, Brightness, Proj\_Sub,  
Stop\_cond ---> HLS

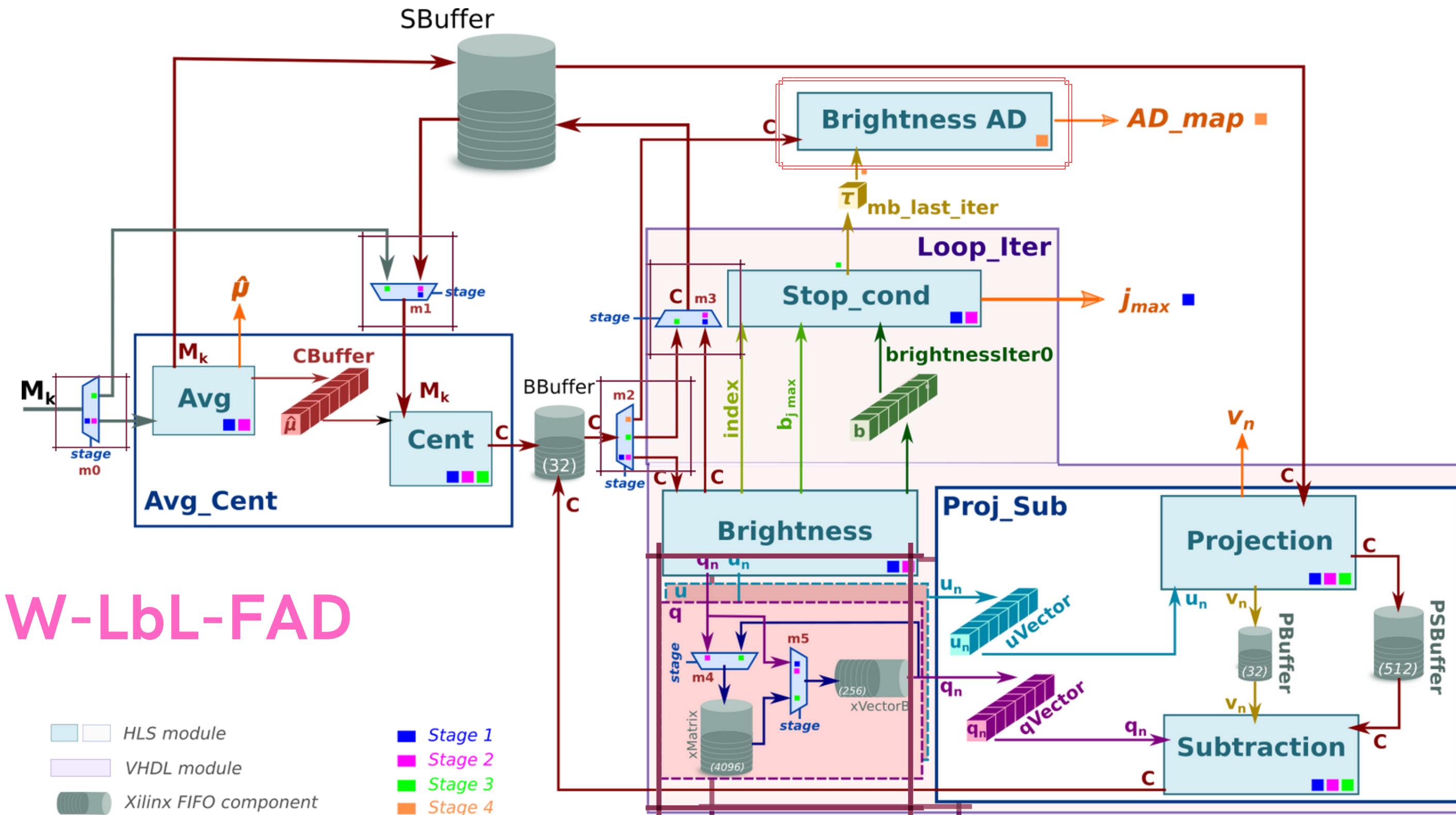
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Hybrid solution  
HLS + VHDL

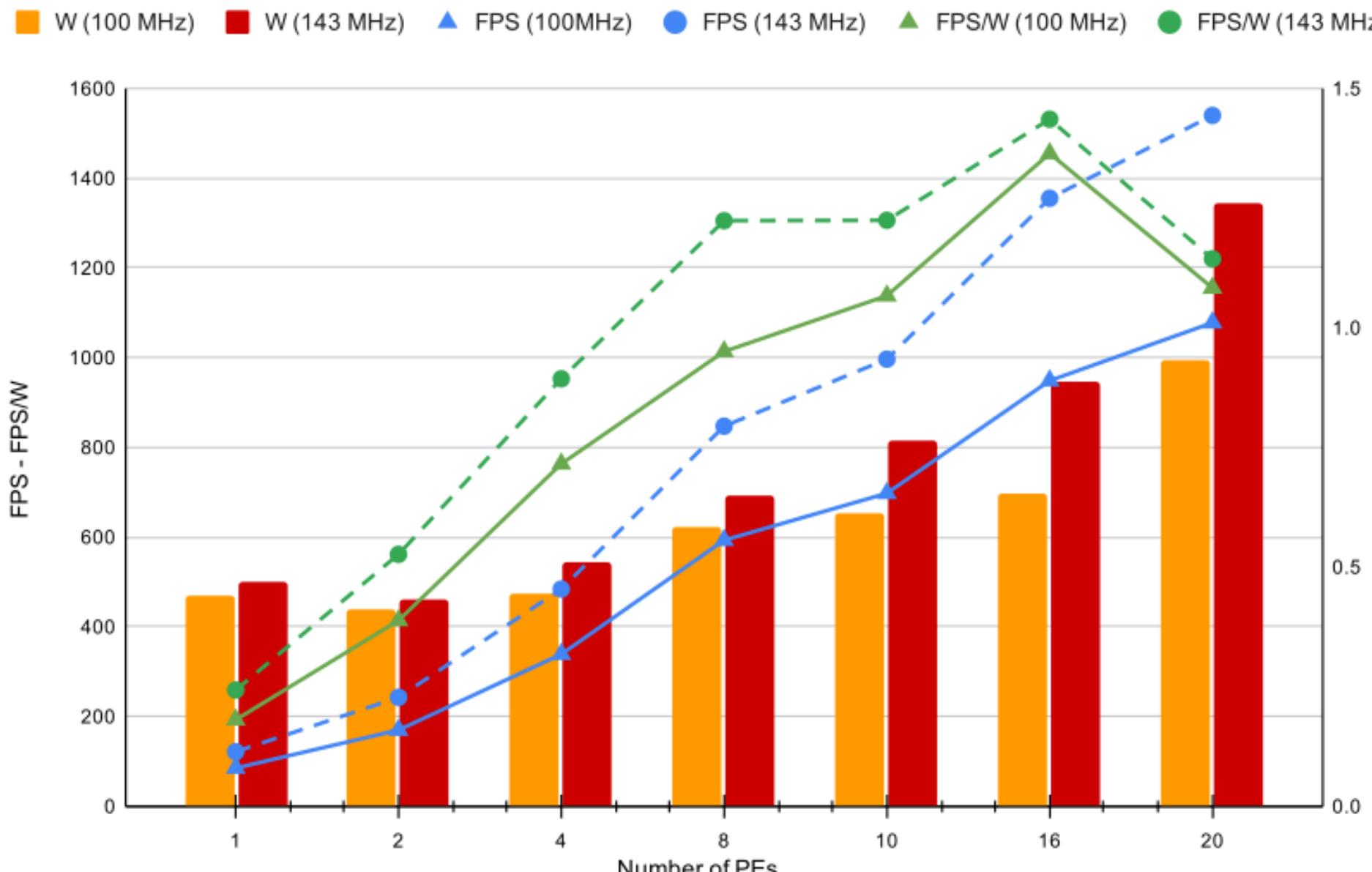
# FPGA-BASED IMPLEMENTATION

FPGA - BASED IMPLEMENTATION

THE HW - LbL - FAD



# EXPERIMENTAL RESULTS



	BS	PEs	BRAM18K	DSP48E	FFs	LUTs
1024	1	107 (76.43%)	14 (6.36%)	8073 (7.59%)	6744 (12.68%)	
	2	91.5 (65.36%)	22 (10%)	8624 (8.11%)	7470 (14.08%)	
	4	95.5 (68.21%)	38 (17.27%)	9981 (9.38%)	9115 (17.13%)	
	8	98.5 (70.36%)	70 (31.82%)	12666(11.90%)	12411(23.33%)	
	10	102.5 (73.21%)	86 (39.09%)	14787 (13.90%)	14856 (27.92%)	
	16	96.5 (68.93%)	134 (60.91%)	18433 (17.32%)	18724 (35.20%)	
	20	98.5 (70.36%)	166 (75.45%)	23071 (21.68%)	23493 (44.16%)	



Sensor	Pixels per frame	Bands per frame	Frames per second	Data resolution
SPECIM FX-10	1024	240/160	330	12 bits/ 16 bits packaged

330

# THE HW-LbL-FAD

Image	Inputs	LbL-FAD		HW-LbL-FAD			
		n <sub>f</sub>	TPR FPR	TPR rFPR	Int32	Int16	Int16-rd
Synthetic Image	20	100	0,00	100 0	100 0	100 2,79	100 0
WASP RIT	60	93,06	0,09	93,06 0,09	93,06 0,09	79,17 0,06	93,06 0,09
AVIRIS WTC	30	43,37	0,02	43,37 0,02	43,37 0,02	44,58 0,02	43,37 0,02

# CONCLUSIONS

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- **Line-by-line anomaly detector**  
... for power-constrained environments such as onboard scenarios.
- **LbL-FAD hardware accelerator**
  - Targeting the XC7Z020-CLG484 version of the Xilinx Zynq-7000SoC due to its low-cost, low-weight and high flexibility.
  - Hybrid solution: combination of HLS generated modules and custom glue logic in VHDL.
- **Real-time performance**  
... since obtained FPS are between 130.11 (PE=1) and 1609.90 (PE=20).
- **Good power-efficiency relation**  
... critical for applications that use remote sensing platforms powered by batteries.

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